# Practice Problems 

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Machine Learning - 2021-I
Maestría en Ing. de Sistemas y Computación

1. Suppose you have 3 data points $x_{1}=(1,2), x_{2}=(3,1)$ and $x_{3}=(0,1)$ and a kernel function $k(x, y)=(\langle x, y\rangle+2)^{2}$
(a) What is the dimension of the feature space $F$ induced by the kernel, and what is the kernel-induced function $\Phi: X \rightarrow F$ ?
(b) Calculate $<\Phi\left(x_{1}\right), \Phi\left(x_{2}\right)>_{F}$ in the feature space.
(c) Calculate the distance between all the data points in the feature space.

## References

[SC04] Shawe-Taylor, J. and Cristianini, N. 2004 Kernel Methods for Pattern Analysis. Cambridge University Press.

